

$$V(t) = 40 \cos(100\pi t + 60^\circ) \text{ V}$$

$$\omega = 100\pi \Rightarrow f = \frac{\omega}{2\pi} = 50 \text{ Hz}$$

a) Find max amplitude

$$V(t) = 40 \text{ V}$$

b) Find Freq in Hz

$$f = 50 \text{ Hz}$$

c) Find Freq in Rad/sec

$$\omega = 100\pi \text{ Rad/sec}$$

d) What is phase angle in radians?

$$\theta = 60^\circ = \left(\frac{60}{360}\right) 2\pi = \frac{\pi}{3} \text{ radians}$$

e) What is phase angle in degrees?

$$\theta = 60^\circ$$

f) What is period in ms? $T = \frac{1}{f} = \frac{1}{50} = 20 \text{ ms}$

g) What is first time after $t=0$ that $v = -40 \text{ V}$

$$-40 = 40 \cos(100\pi t + 60^\circ) \quad \text{Solving: } t = 6.667 \text{ ms}$$

h) $V(t)$ is shifted $\frac{1}{3} \text{ ms}$ to the right. What is the new expression for $V(t)$?

$$\frac{1}{3} \text{ ms is } \frac{1}{6} \text{ of a period} = 60^\circ$$

$$V(t) = 40 \cos(100\pi t + 60^\circ - 60^\circ) \text{ V}$$

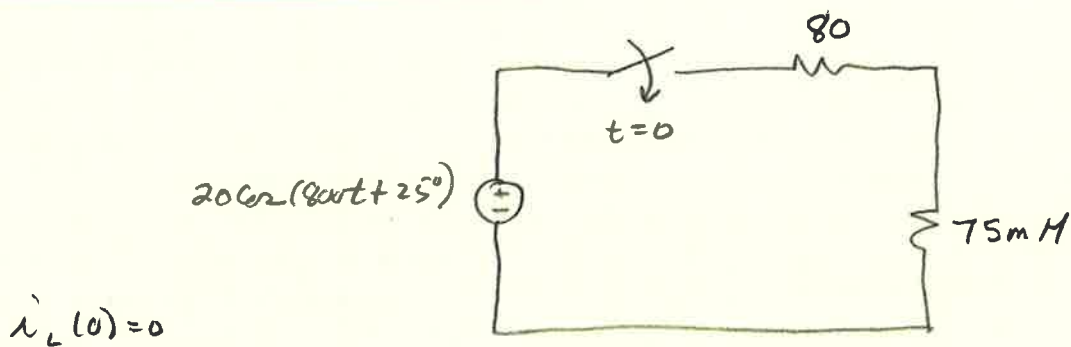
$$V(t) = 40 \cos(100\pi t) \text{ V}$$

i) What is the minimum number of ms that $V(t)$ must be shifted to the left such that $V(t) = 40 \sin(100\pi t) \text{ V}$?

$$\text{Use } \cos(\omega t) = \sin(\omega t + 90^\circ)$$

$$\text{So } V(t) = 40 \sin(100\pi t + 60^\circ + 90^\circ)$$

$$\text{So we have to shift } -150^\circ \text{ or } \frac{210}{360} (20 \text{ ms}) = 11.67 \text{ ms}$$



Eg 9.7 page 323:

$$i = \frac{-V_m}{\sqrt{R^2 + \omega^2 L^2}} \cos(\phi - \theta) e^{-(R/L)t} + \frac{V_m}{\sqrt{R^2 + \omega^2 L^2}} \cos(\omega t + \phi - \theta)$$

where $\theta = \tan^{-1} \frac{\omega L}{R}$

a) find $i(t)$ for $t \geq 0$

from above equation: $V_m = 20$ $R/L = 1066.67$ $\omega L = 60$
 $\sqrt{R^2 + \omega^2 L^2} = 100$
 $\phi = 25^\circ$ $\theta = \tan^{-1} \frac{60}{80} = 36.87^\circ$

$$i(t) = (-195.72 e^{-1066.67t} + 200 \cos(800t - 11.87^\circ)) \text{ mA} \quad t \geq 0$$

b) Find transient + steady state parts

$$\begin{array}{l} \text{transient} : -195.72 e^{-1066.67t} \text{ mA} \\ \text{SS} : 200 \cos(800t - 11.87^\circ) \text{ mA} \end{array}$$

c) find i @ $t = 1.875 \text{ ms}$

$$i(1.875 \text{ ms}) = 28.39 \text{ mA}$$

d) what are maximum amplitude, frequency (rad/sec) + phase of the SS current?

$$\text{max amp} = 200 \text{ mA} \quad \text{freq} = 800 \text{ rad/s} \quad \theta = -11.87^\circ$$

e) By how many degrees are the voltage + SS current out of phase?

$$\text{phase difference} = 25 - (-11.87) = 36.87^\circ$$

current lags voltage

a 400 Hz sinusoidal voltage with a maximum amplitude of 100 V at $t=0$ is applied across an inductor. The maximum amplitude of the steady state current is 20 A.

a) what is the frequency of I_L ?

$$f_{I_L} = 400 \text{ Hz}$$

b) If $\theta_V = 0^\circ$, what is θ_I ?

The current lags the voltage by 90° so $\theta_I = -90^\circ$

c) what is the inductive reactance of L ?

$$\text{Ind react} = \omega L = (2\pi 400)(L) = \frac{V}{I} = \frac{100}{20}$$

$$L = 1.99 \text{ mH}$$

$$\text{Ind react} = 5 \Omega$$

d) what is L ?

$$L = 1.99 \text{ mH}$$

e) what is Z_L ?

$$Z_L = j\omega L = j5 \Omega$$